

# LARNet: Lie Algebra Residual Network for Face Recognition

Xiaolong Yang, Xiaohong Jia, Dihong Gong, Dong-Ming Yan, Zhifeng Li, Wei Liu



AMSS,CAS



UCAS



Tencent Data Platform



CASIA

# Introduction

- A major challenge in practical face recognition applications lies in **significant variations** between **profile and frontal** faces.



**NOT EASY** for face recognition  
with large pose or profile faces !

## □ Traditional techniques:



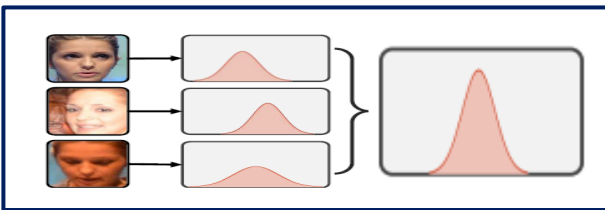
Masi et al. (2016)

- Enrich sources by the synthesis of profile faces
- Unnecessary computational burdens



Rotate-and-Render (2020)

- Frontalize faces under all pose ranges
- Occlusions and non-rigid expressions

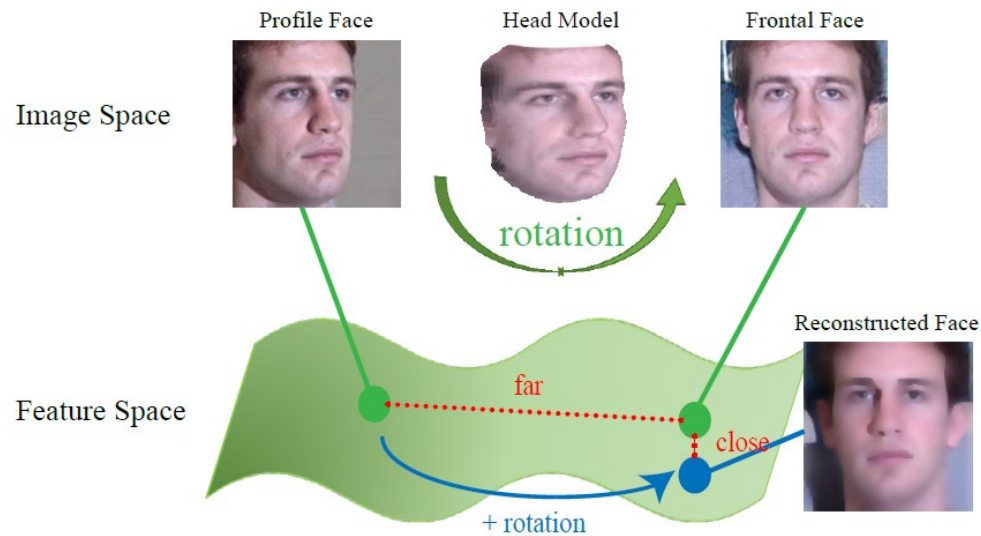


Probabilistic Face Embeddings (2019)

- Represent face images as a Gaussian distribution
- Overly strong hypothesis prior

# Our method

- We explore how face **rotation** in the 3D space affects the deep **feature** generation process.



The difference between frontal and profile face images  
→ Head **rotation** in 3D space

Face recognition for images  
→ Clustering in the deep **feature** space

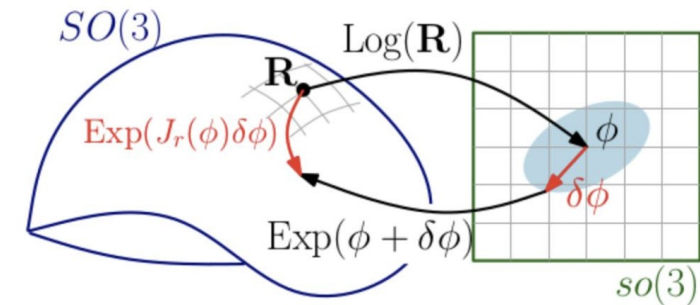
# Our method

□ Rotation matrices are not easy to be embedded in CNNs.

■ Rotation group is **not completely closed**.

$$\forall R_1, R_2 \in SO(3), R_1 \cdot R_2 \in SO(3) \quad \checkmark$$

$$\forall R_1, R_2 \in SO(3), R_1 + R_2 \in SO(3) \quad \times$$



□ New tools – **Lie group and Lie algebra**

■ closed under addition and multiplication operations → Lie group

■ derivable → smooth and continuous → Lie group (differential manifold)

■ derivative operation → tangent space of Lie group → Lie algebra

■ non-linear optimization → Lie algebra attached to the vector space

# Our method

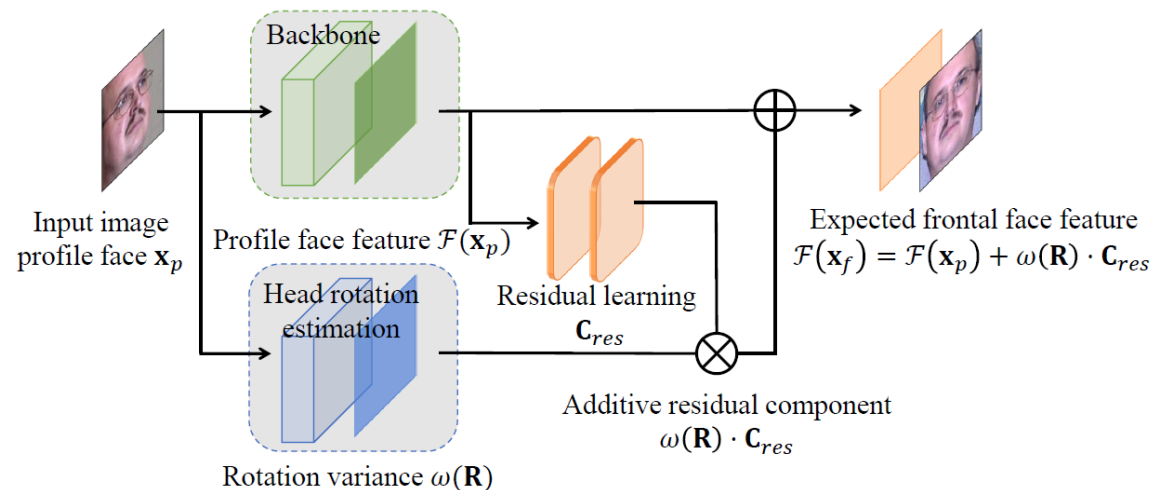
- The frontal-profile face feature pairs in ResNet based on the Lie algebra theory:

$$\mathcal{F}(\mathbf{x}_f) \approx \mathcal{F}(\mathbf{x}_p) + \mathcal{R}_{map}^{-1}(\mathcal{F}(\mathbf{x}_p) - \mathcal{R}_{map}\mathcal{F}(\mathbf{x}_p))$$

$$\mathcal{F}(\mathbf{x}_f) = \mathcal{F}(\mathbf{x}_p) + \omega(\mathbf{R}) \cdot \mathbf{C}_{res}(\mathbf{R}, \mathbf{x}_p)$$

- $\mathbf{C}_{res}$  : a residual subnet for decoding rotation information from input face images
- $\omega(\mathbf{R})$ : a gating subnet to learn rotation magnitude for controlling the strength of  $\mathbf{C}_{res}$

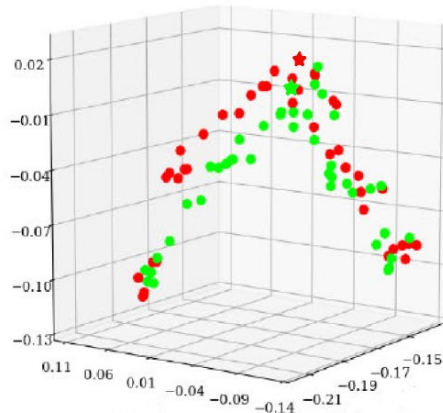
- Our succinct architecture:



# Visualization results – feature distributions



(a) A ground-truth image sequence: pose varirant is from  $-90^\circ$  to  $90^\circ$ .



☆ indicates frontal face ○ indicates profile face  
 Red: the feature distribution of GT image sequence  
 Green: the feature distribution of ours  
 (frontal face image  $0^\circ$  + gating control function)

(b) The feature distributions in the deep feature space

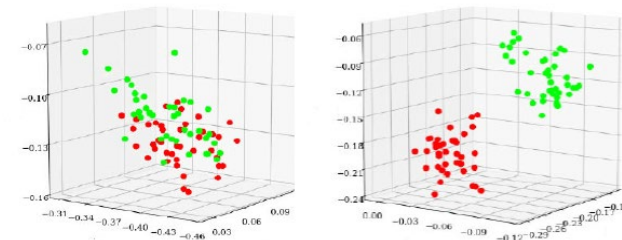
false positive pair



frontal face data



profile face data



The feature distributions of the other method (left) and ours (right)

## □ Feature Representation

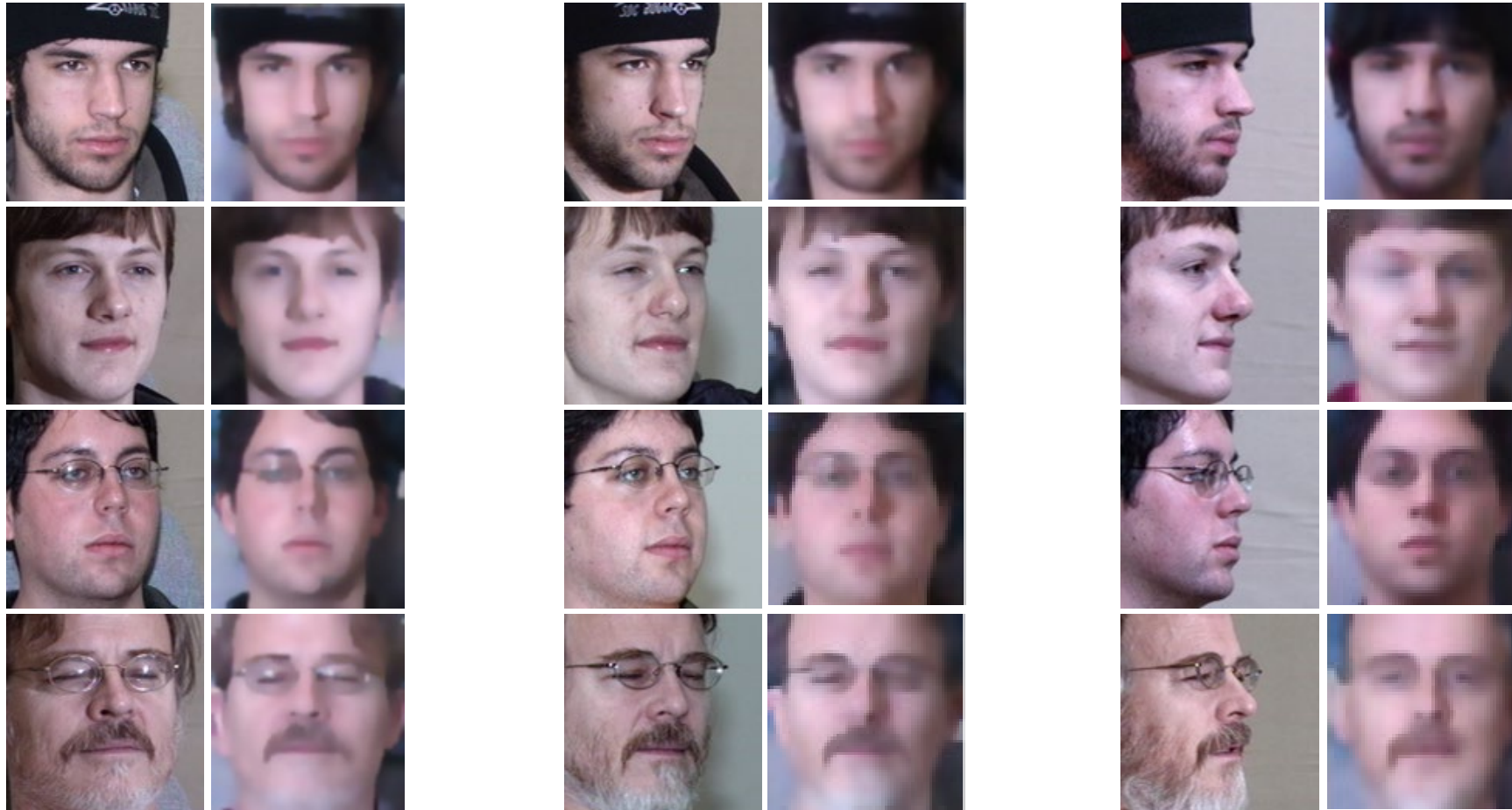
different-pose samples with the same identity

## □ Feature Clustering

different-pose samples with the different identities



# Visualization results – reconstructed faces



15° profile faces

45° profile faces

60° profile faces



# Quantitative evaluation

Method	TAR@FAR=0.01	TAR@FAR=0.001	Rank-1 Acc.	Rank-5 Acc.
Wang <i>et al.</i> (2016)	0.729	0.510	0.822	0.931
Pooling Faces (Hassner <i>et al.</i> , 2016)	0.819	0.631	0.846	0.933
Multi Pose-Aware (AbdAlmageed <i>et al.</i> , 2016)	0.787	—	0.846	0.927
DCNN Fusion (f.) (Chen <i>et al.</i> , 2016)	0.838	—	0.903	0.965
PAMs (Masi <i>et al.</i> , 2016a)	0.826	0.652	0.840	0.925
Augmentation+Rendered (Masi <i>et al.</i> , 2016b)	0.886	0.725	0.906	0.962
Multi-task learning (Yin & Liu, 2017)	0.787	—	0.858	0.938
TPE(f.) (Sankaranarayanan <i>et al.</i> , 2017)	0.900	0.813	0.932	—
DR-GAN (Tran <i>et al.</i> , 2017)	0.831	0.699	0.901	0.953
FF-GAN (Yin <i>et al.</i> , 2017)	0.852	0.663	0.902	0.954
NAN (Yang <i>et al.</i> , 2017)	0.921	0.861	0.938	0.960
Multicolumn (Xie & Zisserma, 2018)	0.920	—	—	—
VGGFace2 (Cao <i>et al.</i> , 2018b)	0.904	—	—	—
Template Adaptation(f.) (Crosswhite <i>et al.</i> , 2018)	0.939	—	0.928	—
DREAM (Cao <i>et al.</i> , 2018a)	0.872	0.712	0.915	0.962
DREAM(E2E+retrain,f.) (Cao <i>et al.</i> , 2018a)	0.934	0.836	0.939	0.960
FTL with 60K parameters (o.s.) (Yin <i>et al.</i> , 2019)	0.864	0.744	0.893	0.947
PFEs (Shi & Jain, 2019)	0.944	—	—	—
DebFace (Gong <i>et al.</i> , 2020)	0.902	—	—	—
Rotate-and-Render (Zhou <i>et al.</i> , 2020)	0.920	0.825	—	—
HPDA (Wang <i>et al.</i> , 2020)	0.876	0.803	0.84	0.88
CDA (Wang & Deng, 2020)	0.911	0.823	0.936	0.957
LARNet	0.941	0.842	0.936	0.968
LARNet+	<b>0.951</b>	<b>0.874</b>	<b>0.949</b>	<b>0.971</b>

## Quantitative evaluation on IJB-A dataset

Our results **surpass** many competitors in the recent 5 years under **all 4 evaluation criteria**:

### Verification task

achieve **95%+** under TAR@FAR=0.01

& **87%+** under TAR@FAR=0.001

### Identification task

achieve **95%** under Rank-1 recognition accuracy

& **97%+** under Rank-5 recognition accuracy

# Quantitative evaluation

- Quantitative evaluation on CFP-FP dataset
- Quantitative evaluation on LFW, YTF, and CPLFW datasets

Method	Verification (%)
SphereFace (o.s.+f.)	94.17
CosFace (o.s.)	94.40
ArcFace (o.s.+f.)	94.04
URFace (all modules, MS1MV2, o.s.)	98.64
Human-level	98.92
LARNet	98.84
LARNet+	<b>99.21</b>

Method	LFW	YTF	CPLFW
HUMAN-Individual	97.27	-	81.21
HUMAN-Fusion	<b>99.85</b>	-	85.24
DeepID (Sun et al., 2014)	99.47	93.20	-
Deep Face (Taigman et al., 2014)	97.35	91.4	-
VGG Face (Parkhi et al., 2015)	98.95	97.30	90.57
FaceNet (Schroff et al., 2015)	99.63	95.10	-
Baidu (Liu et al., 2015a)	99.13	-	-
Center Loss (Wen et al., 2016)	99.28	94.9	85.48
Range Loss (Zhang et al., 2017)	99.52	93.70	-
Marginal Loss (Deng et al., 2017)	99.48	95.98	-
SphereFace(o.s.) (Liu et al., 2017)	99.42	95.0	81.4
SphereFace+(o.s.)	99.47	-	90.30
CosFace(o.s.) (Wang et al., 2018a)	99.51	96.1	-
CosFace*(MS1MV2,R64, o.s.)	99.73	97.6	-
Arcface(o.s.) (Deng et al., 2019)	99.53	-	92.08
ArcFace*(MS1MV2,R100,f.)	99.83	<b>98.02</b>	95.45
Ours: LARNet	99.36	96.55	95.51
Ours: LARNet+	99.71	97.63	<b>96.23</b>

- The first result achieves 99%+ on CFP-FP dataset.
- The first result surpasses the reported human-level.
- Our method also outperforms on general face recognition datasets.

---

THANKS

# LARNet: Lie Algebra Residual Network for Face Recognition



[yangxiaolong17@mails.ucas.ac.cn](mailto:yangxiaolong17@mails.ucas.ac.cn)



[paradocx.github.io](https://github.com/paradocx)



[Paper Homepage](#)

QR Code

---